#### FINITE ELEMENT ANALYSIS

### Subject Code: 13ME2202

L P C 4 0 3

**Pre requisites:** Engineering mechanics and Mechanics of solids **Course Educational Objectives:** 

To make the student

- 1. understand the fundamental concepts and techniques of finite elements
- 2. learn Direct stiffness, Rayleigh-Ritz, Galerkin methods used in FEM
- 3. learn finite element formulation in solid mechanics and heat transfer problems
- 4. know the tools for analyzing engineering problems using FEM and typical commercial FEA package

## **Course Outcomes:**

The student will be able to

- 1. apply concepts and methods of FEA
- 2. apply direct stiffness, Rayleigh-Ritz, Galerkin methods
- 3. formulate and analyze static, dynamic problems of solid mechanics and also heat transfer problems
- 4. use isoparametric, sub parametric and super parametric elements for modeling
- 5. analyze linear and nonlinear problems

## UNIT-I

Introduction, comparison of FEM with other methods, Variational approach, Galerkin Methods. principle of minimum potential energy

Rayleigh- Ritz method, shape functions and characteristics, properties of stiffness matrix, treatment of boundary conditions, Convergence: requirements for convergence, h refinement and p-refinement, basic equations of elasticity, strain displacement relations.

## UNIT –II

1-D structural problems – axial bar element – stiffness matrix, load vector, Trusses: Plane trusses, element stiffness matrix, assembly of global stiffness matrix, load vector, stress calculations

Two-dimensional problems using CST: FE modelling, isoparametric representation, PE approach, element stiffness, force terms, stress calculations, axisymmetric formulation, FE Modelling using CST- PE approach, body force terms, surface traction, stress calculations, cylinder subjected to internal pressure, infinite cylinder.

#### UNIT-III

Isoparametric formulation: 4-noded quadrilateral and its shape functions, element stiffness matrix, element force vectors, Numerical Integration-1D and 2D integrations, stiffness integration, stress calculations, nine -node quadrilateral, eight-node quadrilateral, six-node triangle, sub parametric, super parametric elements, serendipity elements.

# UNIT-IV

Beams and frames: finite element formulation, load vector, boundary considerations, shear force and bending moment, and plane frames Scalar field problems: steady state heat transfer-one-dimensional heat conduction, one-dimensional heat transfer in thin films.

### UNIT-V

Dynamic analysis and nonlinear FEA: formulation-solid body with distributed mass, element mass matrices, evaluation of Eigen values and Eigen vectors for a stepped bar and a beam, introduction to non-linear problems, geometric nonlinearity, material non linearity non-linear dynamic problems, analytical problems

# **TEXT BOOKS:**

- 1. S.S. Rao, *"The finite element method in Engineering"*,3e, Butterworth and Heinnemann, 2001.
- 2. Tirupathi K.Chandrupatla and Ashok D.Belegundu, "*Introduction to finite elements in engineering*", 3e, Pearson Education, 2010.
- 3. O. P. Gupta, *"Finite and boundary element methods in Engineering"*, 2e, Taylor and Francis, 1999.

## **REFERENCES:**

- 1. Robert Cook , "Concepts and applications of finite element analysis", 4e, John Wiley and sons, 2009.
- 2. J. N. Reddy, " *An Introduction to Finite Element Methods*",2e, McGraw Hill,2009.
- 3. O.C. Zienkowitz, "*The Finite element method in engineering science*", 3e, McGraw Hill, 2010.
- 4. K.J Bathe, "Finite Element Procedures in Engineering analysis", 1e, PHI, 2009.
- 5. C.S.Krishnamoorthy, "Finite Element Analysis Theory and Programming", 2e, Mc Graw Hill, 2009.